

# Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>: A Monoclinic Phase in the System Bi<sub>2</sub>O<sub>3</sub>–La<sub>2</sub>O<sub>3</sub>

X. L. Chen<sup>1</sup> and W. Eysel<sup>2</sup>

*Mineralogisches Institut, Universität Heidelberg, 69120 Heidelberg, Germany*

and

J. Q. Li

*Max-Planck-Institut für Festkörperforschung, 70569 Stuttgart, Germany*

Received December 6, 1995; in revised form April 4, 1996; accepted April 10, 1996

The binary system Bi<sub>2</sub>O<sub>3</sub>–La<sub>2</sub>O<sub>3</sub> with La<sub>2</sub>O<sub>3</sub> ≥ 50 mole% has been investigated at 950–1000°C. The results revealed three compounds: Bi<sub>8</sub>La<sub>10</sub>O<sub>27</sub>, Bi<sub>2,4</sub>La<sub>3,6</sub>O<sub>9</sub>, and Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>. Bi<sub>2,4</sub>La<sub>3,6</sub>O<sub>9</sub> has a rhombohedral subcell with hexagonal lattice parameters  $a = 3.96017(5)$  Å,  $c = 9.9691(2)$  Å, and space group  $R3m$ . It is probably the same phase which was reported previously as Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub> (Refs. 5 and 6). Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub> has a monoclinic structure with the subcell lattice parameters  $a = 6.8290(3)$  Å,  $b = 3.9887(1)$  Å,  $c = 4.0524(1)$  Å and  $\beta = 125.094(3)^\circ$  and subcell space group  $C2/m$ . Its average structure has been determined by X-ray powder diffraction and refined by the Rietveld method. The average structure can be described as an oxygen deficient fluorite structure of the  $\delta$ -Bi<sub>2</sub>O<sub>3</sub> type with La and Bi randomly distributed on the cation site. In addition, a superstructure has been observed by TEM. © 1996 Academic Press, Inc.

## INTRODUCTION

The binary systems Bi<sub>2</sub>O<sub>3</sub>–Ln<sub>2</sub>O<sub>3</sub> ( $Ln =$  rare earths) have been widely investigated, particularly for the Bi-rich regions, because  $\delta$ -Bi<sub>2</sub>O<sub>3</sub> and doped Bi<sub>2</sub>O<sub>3</sub> with fluorite-like structures exhibit high ionic conductivity. In the system Bi<sub>2</sub>O<sub>3</sub>–La<sub>2</sub>O<sub>3</sub>, at least four compounds have been reported: a tetragonal phase Bi<sub>1.92</sub>La<sub>0.08</sub>O<sub>3</sub> (1), an fcc phase Bi<sub>1.88</sub>La<sub>0.12</sub>O<sub>3</sub> ( $\delta$ -Bi<sub>2</sub>O<sub>3</sub> type) (2), a rhombohedral phase Bi<sub>0.7</sub>La<sub>0.3</sub>O<sub>1.5</sub> (3), and an orthorhombic phase Bi<sub>8</sub>La<sub>10</sub>O<sub>27</sub> (4). Recently, Wolcyrz and co-workers (5, 6) reported a series of Bi<sub>3</sub>Ln<sub>5</sub>O<sub>12</sub>-type phases ( $Ln =$  La, Pr, Nd, Sm, Eu, Gd, Tb, Dy, Ho, and Y). Among these, the La representative is exceptional in exhibiting a modified composition BiLa<sub>2</sub>O<sub>4.5</sub> = Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>. Its powder pattern was indexed on the basis of a rhombohedral subcell with the hexagonal

lattice parameters  $a = 3.963(1)$  Å,  $c = 9.964(4)$  Å, and space group  $R3m$ . Some additional weak diffraction peaks were explained by the possible superstructure  $a' = 8a = 31.672$  Å and  $c' = 2c = 19.927$  Å (5, 6).

In the present study, Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub> was found to be a new phase with a monoclinic structure. We report here the synthesis and the average structure of this monoclinic phase.

## EXPERIMENTAL

In the system Bi<sub>2</sub>O<sub>3</sub>–La<sub>2</sub>O<sub>3</sub> samples with 50.0, 55.0, 57.5, 60.0, 62.5, 65.0, 66.7, and 80 mole% La<sub>2</sub>O<sub>3</sub> were prepared by solid state reaction from mixtures of La<sub>2</sub>O<sub>3</sub> (Fluka, 99.98%) and Bi<sub>2</sub>O<sub>3</sub> (Heraeus, 99.999%). Before weighing, La<sub>2</sub>O<sub>3</sub> was preheated at 1000°C for 12 h to remove the carbon dioxide and water it absorbs in air. The samples were mixed, ground, and preheated at 800°C for 12 h in air and then fired at 950–1000°C for 5–7 days. Additional annealings for 2 days with intermediate grindings were performed for some samples. The samples were finally quenched to room temperature in air. The weight loss, presumably due to Bi<sub>2</sub>O<sub>3</sub> vaporization during heating, was always less than 0.8% of the total sample weight.

Phase identification, determination of lattice parameters, and the Rietveld refinement were performed on an automated Norelco diffractometer using Ni filtered CuK $\alpha$  radiation at room temperature. All data were collected by step scanning with steps of  $0.02^\circ 2\theta$ . An angular range from  $10^\circ$  to  $70^\circ$  and a measuring time of 1 s were generally applied for phase identification while  $10^\circ$  to  $90^\circ$  and  $\geq 10$ s were used for the lattice parameter determinations. NBS SRM 640 Si was added as internal standard. The lattice parameters were calculated with the program NBS\*AIDS 83(7). For the Rietveld refinement, the data were collected over an angular range of  $25^\circ$  to  $135^\circ$  with a measuring time of 14 s. A total of 5500 points and 96 independent

<sup>1</sup> On leave from Institute of Physics, Chinese Academy of Sciences, Beijing 100080, People's Republic of China.

<sup>2</sup> To who correspondence should be addressed.

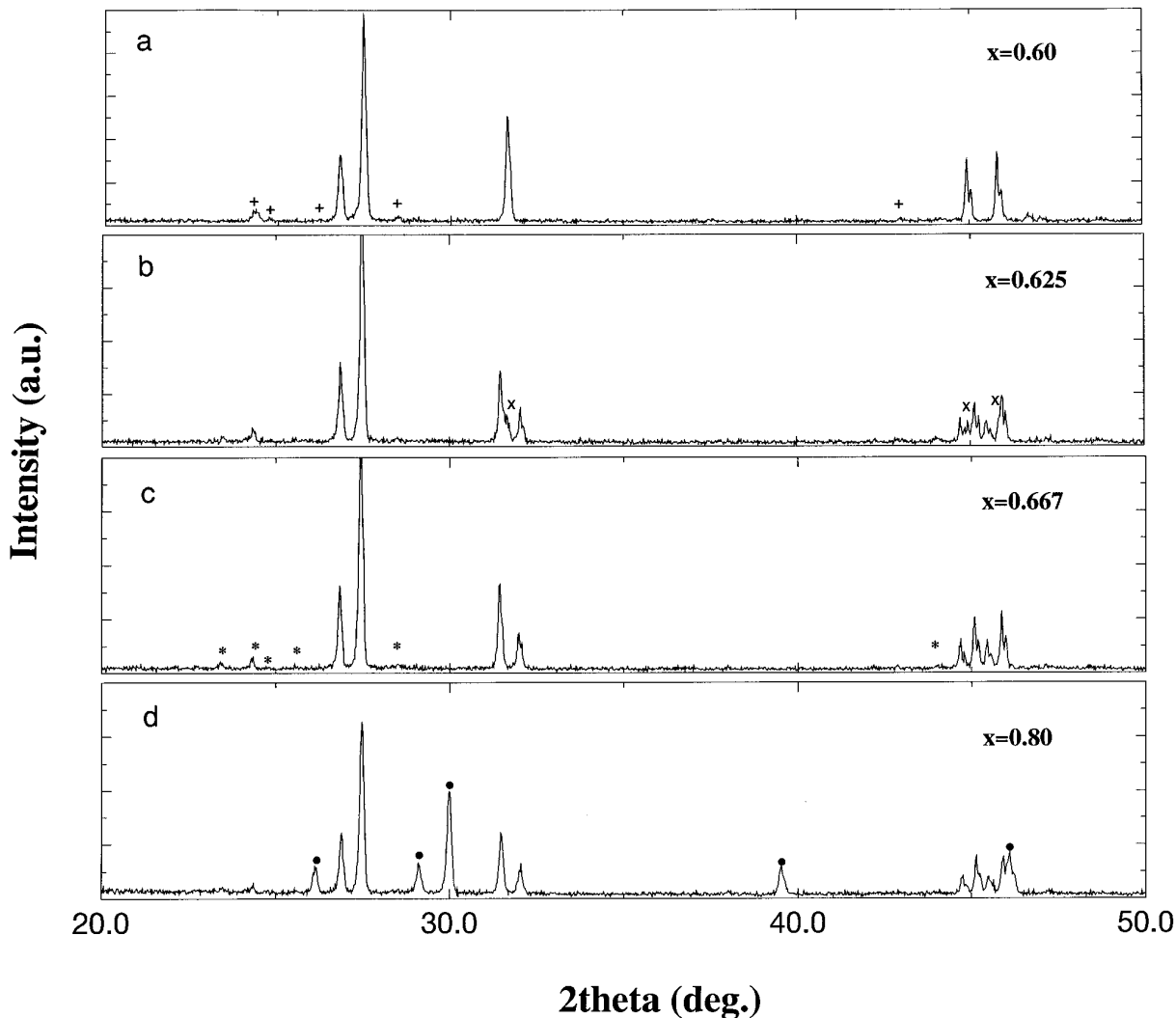


FIG. 1. The X-ray powder diffraction patterns of  $\text{Bi}_{1-x}\text{La}_x\text{O}_{1.5}$ . (a)  $x = 0.60$ , peaks marked by + are due to superstructure lines; (b)  $x = 0.625$ , peaks marked by x are due to  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$ ; (c)  $x = 0.667$ , peaks marked by \* are due to superstructure lines; and (d)  $x = 0.80$ , the peaks marked by small dot are due to  $\text{La}_2\text{O}_3$ .

reflections were measured. The Rietveld refinement was carried out by using the computer program DBW3.2S(8).

## RESULTS

For compositions with  $\text{La}_2\text{O}_3 \geq 50$  mole%, X-ray powder diffraction (XRPD) measurements resulted in the existence of three compounds, namely  $\text{Bi}_8\text{La}_{10}\text{O}_{27}$ ,  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$ , and  $\text{Bi}_2\text{La}_4\text{O}_9$ .  $\text{Bi}_8\text{La}_{10}\text{O}_{27}$  crystallizes in the space group  $Immm$  with  $a = 12.083(4)$  Å,  $b = 16.340(1)$  Å, and  $c = 4.0989(2)$  Å. This is in good agreement with the previous data (4). The diffraction pattern of  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$  (Fig. 1a) agrees well with that reported for  $\text{Bi}_2\text{La}_4\text{O}_9$  by Wolcyrz and co-workers (5, 6). Its main diffraction peaks can be indexed using a rhombohedral cell with

hexagonal lattice parameters  $a = 3.96017(5)$  Å and  $c = 9.9691(2)$  Å. The observed conditions for reflections are  $-h + k + l = 3n$  for  $hkl$ ,  $l = 3n$  for  $hhl$ , and  $l = 3n$  for  $00l$ , resulting in the possible space groups  $R\bar{3}m$  and  $R3m$ .  $R3m$  is rather probable since it agrees with that of the closely related  $\text{BiO}$  (9). Some unindexed weak diffraction peaks (Fig. 1a) are due to the proposed superstructure  $8a \times 2c$  (6). At 66.7 mole%  $\text{La}_2\text{O}_3$ , a new compound  $\text{Bi}_2\text{La}_4\text{O}_9$  was found. Figure 1c shows its XRPD pattern. Although its composition is very close to  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$ , it obviously is a different phase. Figure 1b shows the XRPD pattern for the sample with 62.5 mole%  $\text{La}_2\text{O}_3$ . It consists of the diffraction peaks of  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$  and  $\text{Bi}_2\text{La}_4\text{O}_9$ . This excludes that both are members of a solid solution series. Figure 1d shows the XRPD pattern for the sample with

TABLE 1  
The Powder Data of  $\text{Bi}_2\text{La}_4\text{O}_9$

$d_{\text{cal}}$	$d_{\text{obs}}$	$I_{\text{rel}}(\%)$	$h k l$	$d_{\text{calc}}$	$d_{\text{obs}}$	$I_{\text{rel}}(\%)$	$h k l$
	4.964	5	*		1.4353	2	*
	3.795	4	*	1.4212	1.4212	6	-2 2 2
	3.659	6	*	1.3969	1.3968	3	4 0 0
	3.594	4	*	1.3195	1.3194	2	-2 0 3
	3.474	4	*	1.3098	1.3099	3	1 1 2
3.3157	3.3154	35	0 0 1	1.3060	1.3059	3	-4 0 3
3.2464, 3.2453	3.2459	100	1 1 0, -2 0 1	1.2968	1.2968	3	2 2 1
2.8424	2.8423	35	-1 1 1	1.2935	1.2936	5	1 3 0
2.7938	2.7938	18	2 0 0	1.2839, 1.2837	1.2839	6	-4 2 1, -5 1 2
	2.0544	3	*	1.2791	1.2791	4	-3 1 3
2.0257	2.0255	12	-2 0 2	1.2749	1.2750	3	0 2 2
2.0084	2.0084	18	1 1 1	1.2633	1.2634	3	-1 3 1
1.9943	1.9944	12	0 2 0	1.2616	1.2616	3	3 1 1
1.9768	1.9767	20	-3 1 1	1.2587	1.2586	4	-4 2 2
1.7288	1.7287	9	-1 1 2	1.1726	1.1726	2	-1 1 3
1.7090, 1.7085	1.7086	18	0 2 1, -3 1 2	1.1541	1.1542	4	1 3 1
1.6991	1.6990	10	-2 2 1	1.1537	1.1537	4	-5 1 3
1.6876	1.6877	9	3 1 0	1.1480	1.1481	3	-3 3 1
1.6779	1.6778	6	-4 0 1	1.1441	1.1442	3	4 2 0
1.6579	1.6579	4	0 0 2	1.1380	1.1379	2	-6 0 2
1.6232, 1.6226	1.6231	10	2 2 0, -4 0 2	1.1004	1.1005	2	-2 2 3
	1.6093	3	*	1.0928, 1.0926	1.0926	3	-1 3 2, -4 2 3

Note. For the indexed subcell, the Smith/Snyder Figure of Merit  $F(30) = 197.7(0.004, 38)$  (10). Reflections marked by \* are due to the superstructure. (The data were submitted to ICDD for publication in the PDF.)

80.0 mole%  $\text{La}_2\text{O}_3$ . It contains the peaks of both  $\text{Bi}_2\text{La}_4\text{O}_9$  and  $\text{La}_2\text{O}_3$ . This also demonstrates that  $\text{Bi}_2\text{La}_4\text{O}_9$  coexists with  $\text{La}_2\text{O}_3$  in the compositional range from  $x = 66.7$  to 100 mole%  $\text{La}_2\text{O}_3$ . The observations clearly indicate that  $\text{Bi}_2\text{La}_4\text{O}_9$  is a distinct compound with an individual structure.

$\text{Bi}_2\text{La}_4\text{O}_9$  is a stable compound. DTA results showed that it has no measurable phase transition up to  $1100^\circ\text{C}$ . The compound melts above  $1350^\circ\text{C}$ .

Like  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$ , also  $\text{Bi}_2\text{La}_4\text{O}_9$  exhibits some weak un-indexed reflections (Fig. 1c). The main peaks can be indexed using a monoclinic subcell with lattice parameters

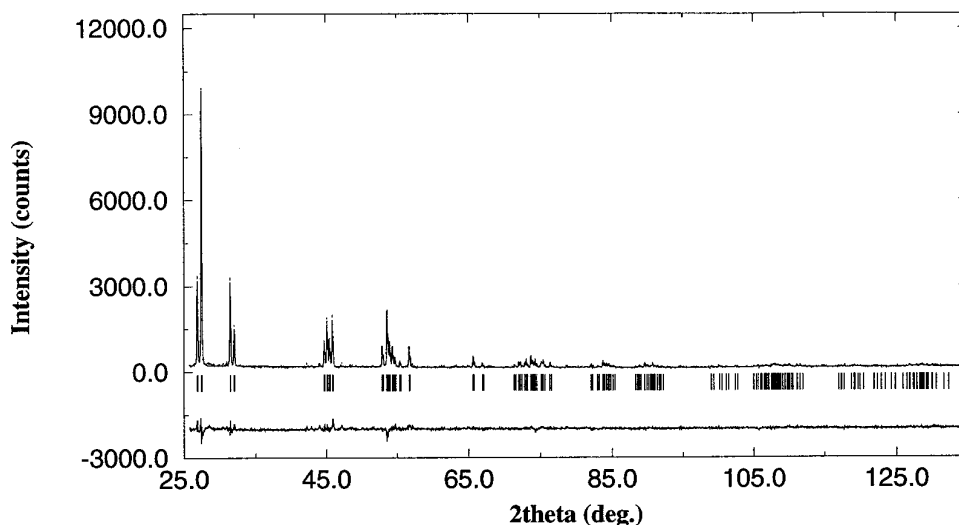


FIG. 2. The Rietveld refinement pattern of  $\text{Bi}_2\text{La}_4\text{O}_9$ . Small points represent the experimental values and solid lines the calculated pattern. The solid line at the bottom is the difference between the experimental and calculated values.

TABLE 2

Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>: Final Rietveld Refined Parameters from X-ray Powder Diffraction Data,  $R_{\text{Bragg}} = 7.9\%$ ,  $R_{\text{wp}} = 11.38\%$ ,  $R_{\text{p}} = 8.66\%$ ,  $R_{\text{exp}} = 6.73\%$

Atom	Site	$x/a$	$y/b$	$z/c$	$B(\text{\AA}^2)$	Occupancy
La	2a	0	0	0	1.8(3)	0.667
Bi						
O	4i	0.282(3)	0	0.741(4)	1.5(5)	0.75

Bond length Bi(La)–O:  $2.46(2) \times 2.235(1) \times 3.267(2) \times 3$

$a = 6.8290(3) \text{ \AA}$ ,  $b = 3.9887(1) \text{ \AA}$ ,  $c = 4.0524(1) \text{ \AA}$ , and  $\beta = 125.094(3)^\circ$ . Table 1 presents its powder data. The observed condition for reflections allow for the space groups  $C2/m$ ,  $C2$ , or  $Cm$ . The cell can be transformed to another setting with  $a = 5.589 \text{ \AA}$ ,  $b = 3.989 \text{ \AA}$ ,  $c = 4.052 \text{ \AA}$ , and  $\beta = 91.30^\circ$ , corresponding to the space groups  $I2/m$ ,  $I2$ , or  $Im$ . It is evident that the cell parameters of this body-centered cell are closely related to that of fluorite type  $\delta\text{-Bi}_2\text{O}_3(\text{fcc})$  by the relations  $b \approx c \approx (\sqrt{2}/2) a_{\text{F}}$ ,  $a \approx a_{\text{F}}$ . Since the unindexed diffraction peaks are weak, the approximate crystal structure could be refined with the subcell.

Because of the apparent close relationship with the fluorite structure, calculations were performed with starting positional parameters according to those of the classical cubic fluorite. The subcell then should contain one (Bi, La)<sub>2</sub>O<sub>3</sub>. Starting with  $C2/m$ , the Bi and La atoms were put statistically on the site  $2a(0, 0, 0)$  with the initial ratio La/Bi = 2.0. The oxygen atoms were set on the site  $4i(x, 0, z)$  with  $x = 0.25$  and  $z = 0.75$ . The

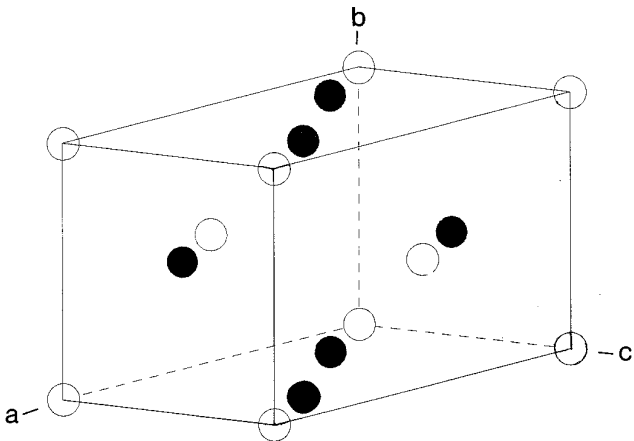


FIG. 3. The crystal structure for Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>. The open circles stand for La or Bi atoms and the filled circles for oxygen.

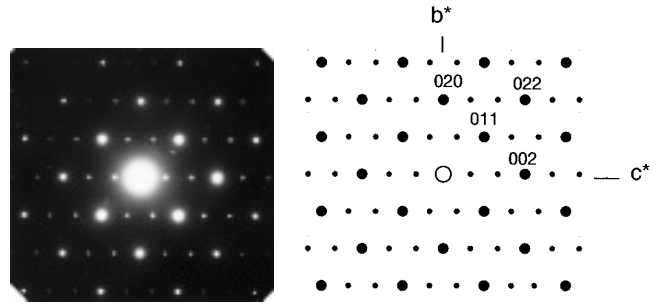


FIG. 4. Electron diffraction pattern of Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>. Indices refer to the body-centered cell. Electron beam is parallel to  $[100]$ . Superstructure along  $[001]$  with a period  $3 \times c$  (horizontal direction).

occupancy factor for oxygen was set to 0.75, corresponding to 3 oxygen atoms in the cell. Under these conditions and with the isotropic thermal parameters fixed to  $1 \text{ \AA}^2$ , the agreement factor of the initial refinement  $R_{\text{wp}}$  was 18.3%. Successive refinements of the positional parameters of oxygen and the isotropic thermal parameters lead to  $R_{\text{wp}} = 11.3\%$ ,  $R_{\text{p}} = 8.77\%$ . At this stage refinement of the ratio Bi/La while keeping their isotropic thermal parameter fixed confirmed that the ratio Bi/La = 1:2. Attempts with space groups  $C2$  and  $Cm$  only yielded larger agreement factors. Hence, the most probable space group is  $C2/m$ . The result of the final Rietveld refinement is plotted in Fig. 2. Table 2 gives the structural parameters of the final refinement. Figure 3 shows the average crystal structure of Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>.

## DISCUSSIONS

The bond lengths for Bi(La)–O range from 2.345 to 2.673  $\text{\AA}$ . These values are in good agreement with the known values. The average coordination number of the cations is 6 as in  $\delta\text{-Bi}_2\text{O}_3$ . The polyhedron, however, is deformed due to some oxygen shift. The isothermal temperature factors  $B$  for (Bi, 2La) and O are  $1.8(5) \text{ \AA}^2$  and  $1.5(5) \text{ \AA}^2$ , respectively. The values are rather large. Comparably large  $B$  values were observed for Bi<sub>0.7</sub>La<sub>0.3</sub>O<sub>1.5</sub> [ $B(\text{La, Bi}) = 0.91\text{--}1.35 \text{ \AA}^2$ ,  $B(\text{O}) = 1.40\text{--}4.93 \text{ \AA}^2$ ] (3) and Bi<sub>8</sub>La<sub>10</sub>O<sub>27</sub> [ $B(\text{La, Bi}) = 1.6\text{--}2.5 \text{ \AA}^2$ ,  $B(\text{O}) = 1.9\text{--}6.3 \text{ \AA}^2$ ] (4). The large  $B$  values in the present case may be attributed to ordering phenomena. It should be noted that the  $B$  values for La and Bi are larger than those for the light oxygen atoms. Hence, the ordering of the metal atoms is rather probable. Correspondingly, preliminary TEM investigations revealed the existence of a superstructure in Bi<sub>2</sub>La<sub>4</sub>O<sub>9</sub>. Figure 4 shows the electron diffraction pattern along  $[100]$  of the body-centered cell. Strong spots originate from the average structure, while weak spots indicate a possible triple superstructure along  $[001]$  of the body-

centered cell. However, no proper superstructure cell could be found so far which allows to index also all weak X-ray powder diffraction peaks. Further TEM investigations are needed.

In the present study, the hexagonal phase reported for  $\text{Bi}_2\text{La}_4\text{O}_9$  by Horyń *et al.* (5) was also found, but for the slightly different composition  $\text{Bi}_{2.4}\text{La}_{3.6}\text{O}_9$ . This discrepancy may be due to the different syntheses conditions.

On the basis of our results, Wolcyrz *et al.* (private communication, 1996) did some reinvestigations and showed that  $\text{Bi}_2\text{La}_4\text{O}_9$  converts from their hexagonal to our monoclinic structure by annealing it for 13 days at  $900^\circ\text{C}$ . This proves two polymorphic forms, of which the monoclinic structure is obviously the more stable one.

Finally,  $\text{Bi}_2\text{Nd}_4\text{O}_9$  was also synthesized and found to be isostructural to the monoclinic  $\text{Bi}_2\text{La}_4\text{O}_9$ . Its lattice parameters are  $a = 6.7066(3) \text{ \AA}$ ,  $b = 3.9002(2) \text{ \AA}$ ,  $c = 3.9583(2) \text{ \AA}$ , and  $\beta = 125.233(5)^\circ$ . Attempts to synthesize other isostructural compounds with further lanthanide ions failed, indicating that the structure is only stable with the largest cations  $\text{La}^{3+}$  and  $\text{Nd}^{3+}$ .

## ACKNOWLEDGMENTS

The investigations were supported by the Alexander von Humboldt Foundation, the National Natural Science Foundation of China, and the ICDD. We thank H. Maltry for technical help.

## REFERENCES

1. ICDD-PDF No. 41-273.
2. Takahashi, H. Iwahra, and T. Esaka, *J. Electrochem. Soc.* **124**, 1563 (1977).
3. D. Mercurio, M. El Farissi, J. C. Champarnaud-Mesjard, and B. Frit, *J. Solid State Chem.* **80**, 133 (1989).
4. C. Michel, V. Caignaert, and B. Raveau, *J. Solid State Chem.* **90**, 296 (1991).
5. R. Horyń, M. Wolcyrz, and A. Wojakowski, *J. Solid State Chem.* **116**, 68 (1995).
6. M. Wolcyrz, L. Kepiński, and R. Horyń, *J. Solid State Chem.* **116**, 72 (1995).
7. C. R. Hubbard, J. K. Stalick, and A. D. Mighell, "NBS\*AIDS83, A Program for the Analysis and Evolution of Crystallographic Data." NIST, Washington, D.C., 1983.
8. D. B. Wiles and R. A. Young, *J. Appl. Crystallogr.* **14**, 149 (1981).
9. IDCC-PDF No. 27-54.
10. G. S. Smith and R. J. Snyder, *J. Appl. Crystallogr.* **12**, 60 (1979).